

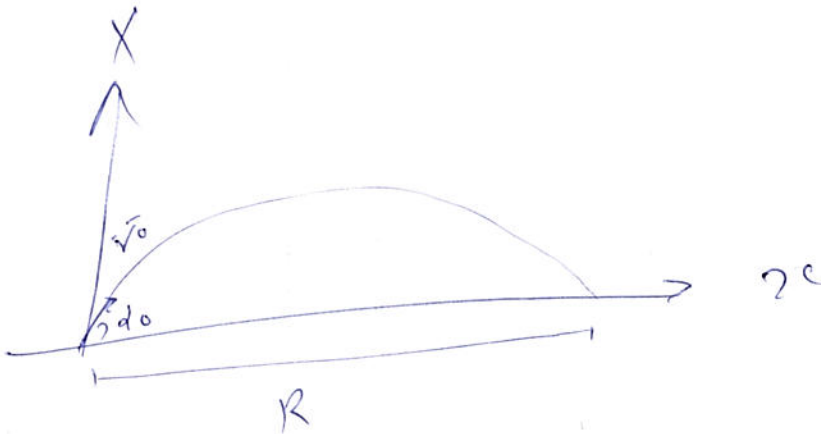
Closed book. No calculators are to be used for this quiz.  
Quiz duration: 10 minutes

Name:

Student ID:

Signature:

A particle is thrown with initial speed  $v_0$  at an angle  $\alpha_0$  with the horizontal axis. Derive the equation giving the horizontal range (horizontal distance from the starting point)  $R$  of the particle as a function of  $v_0$ ,  $\alpha_0$ , and  $g$ . Find out the angle  $\alpha_0$  that will maximize  $R$  for a constant  $v_0$ , explain your answer.



$$0 = -\frac{1}{2}gt^2 + v_0 \sin \alpha_0 t \Rightarrow t = \frac{2v_0 \sin \alpha_0}{g}$$

$$R = v_0 \cos \alpha_0 t = v_0 \cos \alpha_0 \frac{2v_0 \sin \alpha_0}{g}$$

$$\Rightarrow R = \frac{v_0^2 \sin 2\alpha_0}{g}$$

$$\alpha_0 = 45^\circ \Rightarrow \text{max. } R$$

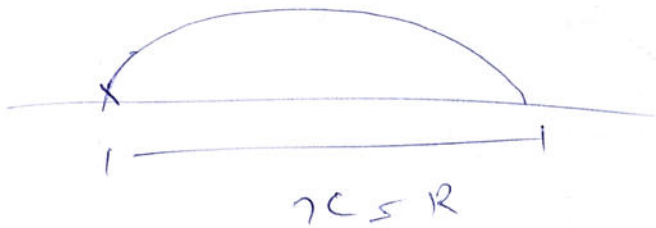
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A demolition crew uses dynamite to blow an old building up. Debris from the explosion flies off in all directions and is later found at distances as far as 50 m from the explosion. Estimate the maximum speed at which debris was blown outward by the explosion. (Ignore the air resistance, take  $g=10 \text{ m/s}^2$ )



$$2545$$

$$R = 50 \text{ m}$$

$$R \leq \frac{v_0^2 \sin^2 \alpha}{g}, \quad \sin^2 \alpha \leq 1$$

$$\Rightarrow v_0 \leq \sqrt{Rg} \leq \sqrt{50 \times 10} \leq 10\sqrt{5} \approx 22 \dots$$

$v_0 \leq \text{max. speed}$

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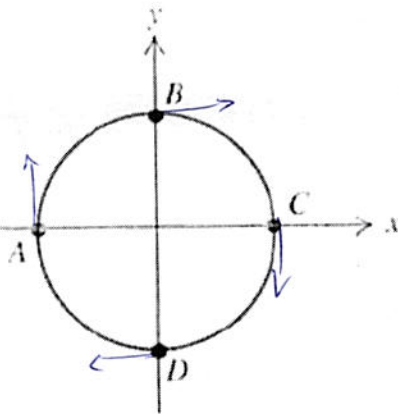
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An athlete starts at point A and runs at a constant speed of 6 m/s around a circular track 100 m in diameter as shown in figure below. Find the x and y components of this runner's average velocity and acceleration between points (a) A and B (b) A and C (c) C and D, and (d) A and A (full lap). (Take  $\pi=3$ )

$$R \leq \frac{100}{2} \leq 50 \text{ (m)}$$

$$2\pi R \leq vT \Rightarrow T = 50$$



$$\vec{v}_{AB} \leq \frac{\vec{v}_B - \vec{v}_A}{T_{1/4}} = \frac{50\hat{y} + 50\hat{x}}{50/4} = 4\hat{y} + 4\hat{x} \quad , \quad \vec{a}_{AB} \leq \frac{\vec{v}_B - \vec{v}_A}{T_{1/4}} = \frac{6\hat{x} - 6\hat{y}}{50/4}$$

$$\vec{v}_{AC} \leq \frac{50\hat{x} + 50\hat{x}}{50/2} = 4\hat{x} \quad , \quad \vec{a}_{AC} \leq \frac{-6\hat{y} - 6\hat{y}}{50/2} = -\frac{12\hat{y}}{50}$$

$$\vec{v}_{CD} \leq \frac{-50\hat{y} - 50\hat{x}}{3T/4} = \frac{-40\hat{y} - 40\hat{x}}{3} \quad , \quad \vec{a}_{CD} \leq \frac{-6\hat{x} + 6\hat{y}}{\frac{3 \times 50}{4}} = \frac{-8\hat{x} + 8\hat{y}}{50}$$

$$\vec{v}_{AA} \leq \frac{-50\hat{x} + 50\hat{x}}{T} = 0 \quad , \quad \vec{a}_{AA} \leq \frac{6\hat{y} - 6\hat{y}}{T} = 0$$

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A model of a helicopter rotor has four blades, each 4 m long from the central shaft to the blade tip. The model is rotated in a wind tunnel at 600 revolutions per minute.

(a) What is the linear speed of the blade tip, in m/s?

(b) What is the radial acceleration of the blade expressed as a multiple of the acceleration of gravity,  $g$ ? (Take  $\pi=3$  and  $g=10 \text{ m/s}^2$ )

~~$f = 600 \times \frac{1}{60} = 10 \text{ Hz}$~~

600 Rev. 1 min.

1 Rev.  $T$  (s)

$\Rightarrow T = \frac{60 \text{ s}}{600} = 0.1 \text{ s}$

$f = 10 \Rightarrow \omega = 20 \text{ rad/s}$

a)  $v = R\omega = 20 \text{ rad/s} \times 4 \text{ m} = 80 \text{ m/s}$

b)  $a = \frac{v^2}{R} = \frac{(80 \text{ m/s})^2}{4 \text{ m}} = \frac{6400 \text{ m}^2/\text{s}^2}{4 \text{ m}}$

$= 1600 \text{ m/s}^2$

$\Rightarrow a = 160 \text{ g}$

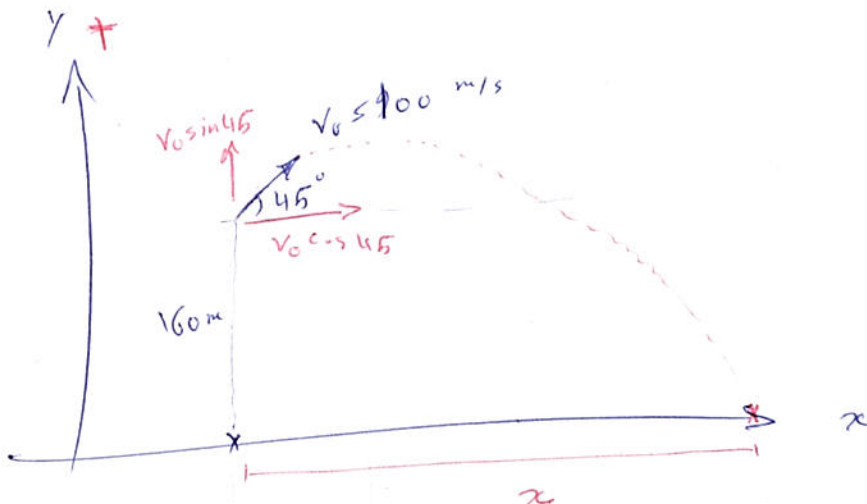
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An airplane is flying with a velocity of 100 m/s at an angle of  $45^\circ$  above the horizontal. When the plane is 160 m directly above a dog that is standing on level ground, a suitcase drops out of the luggage compartment. How far from the dog will the suitcase land? (Ignore the air resistance, take  $g=10 \text{ m/s}^2$  and  $\sin 45^\circ = \cos 45^\circ = 0.7$ )



motion in  $y$  direction:  $\left\{ \begin{array}{l} v_{0y} = v_0 \sin 45 = \frac{100}{\sqrt{2}} = 70 \\ a_y = -g \\ \Delta y = -160 \end{array} \right.$

$$\Delta y = -\frac{1}{2} g t^2 + v_{0y} t$$

$$\Rightarrow -160 = -5 t^2 + \frac{100}{\sqrt{2}} t \Rightarrow 5 t^2 - 70 t - 160 = 0 \Rightarrow \boxed{2516 \text{ (s)}}$$

motion in  $x$  direction:  $\left\{ \begin{array}{l} a_x = 0 \\ v_{0x} = v_0 \cos 45 = 70 \\ \Delta x = ? \end{array} \right.$

$$\Delta x = v_{0x} t = 70 \times 16 = 1120$$